



CMPT 413/713: Natural Language Processing

Classification

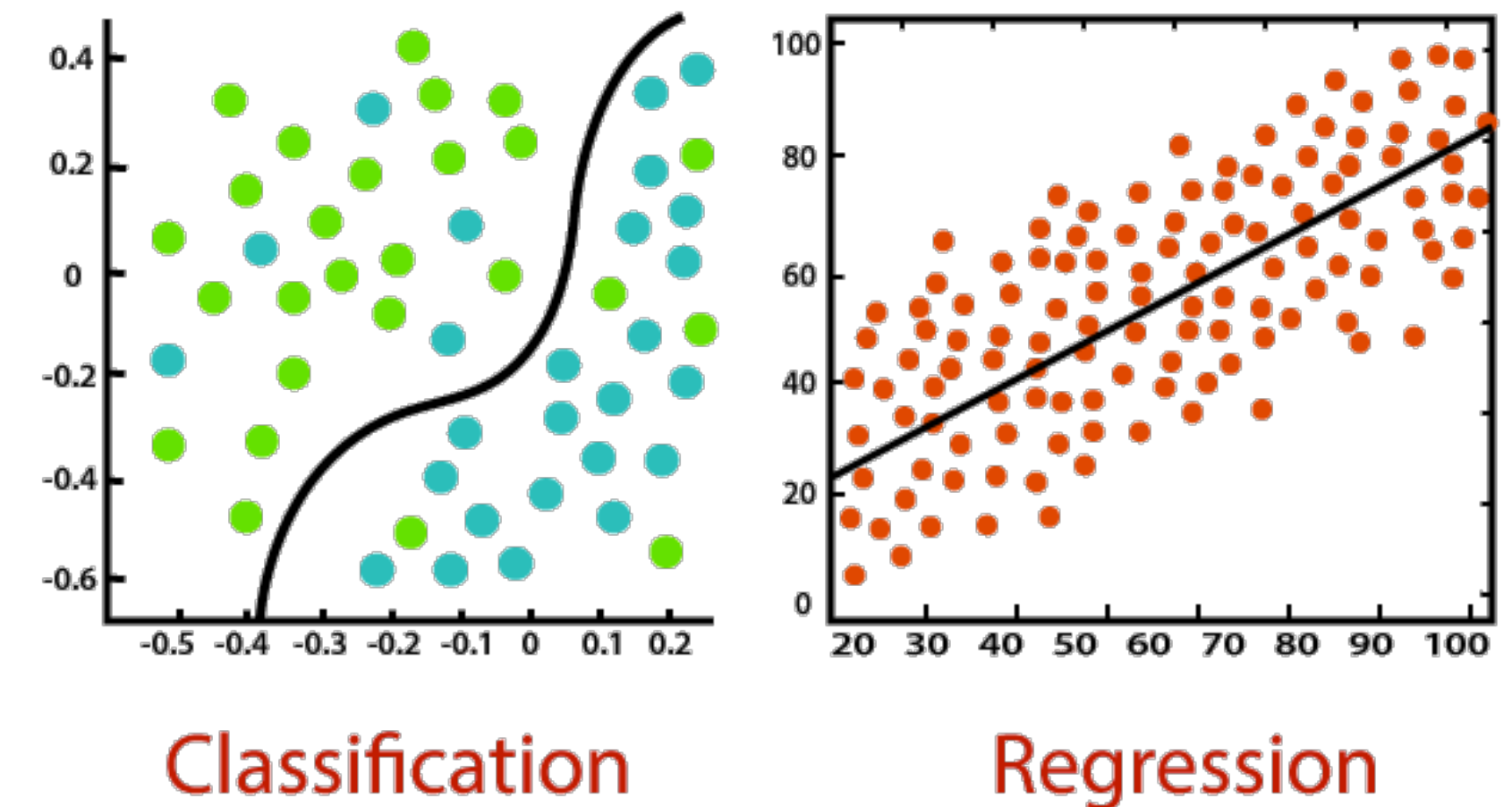
Spring 2026
2026-01-12

Adapted from slides from Danqi Chen, Karthik Narasimhan, and Anoop Sarkar

Review: Basic Machine Learning Terminology

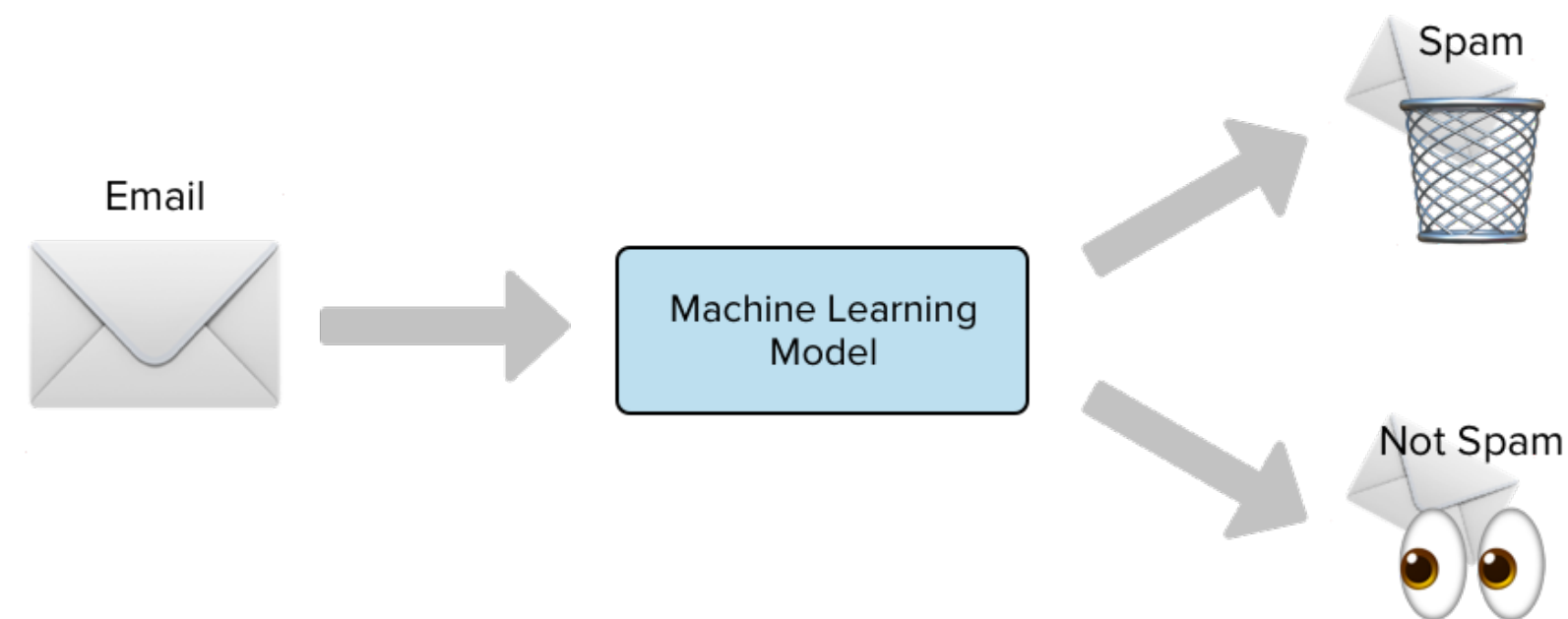
labeled training data

- **Supervised** vs Unsupervised learning
- **Classification** vs Regression
- Discriminative vs **Generative** models

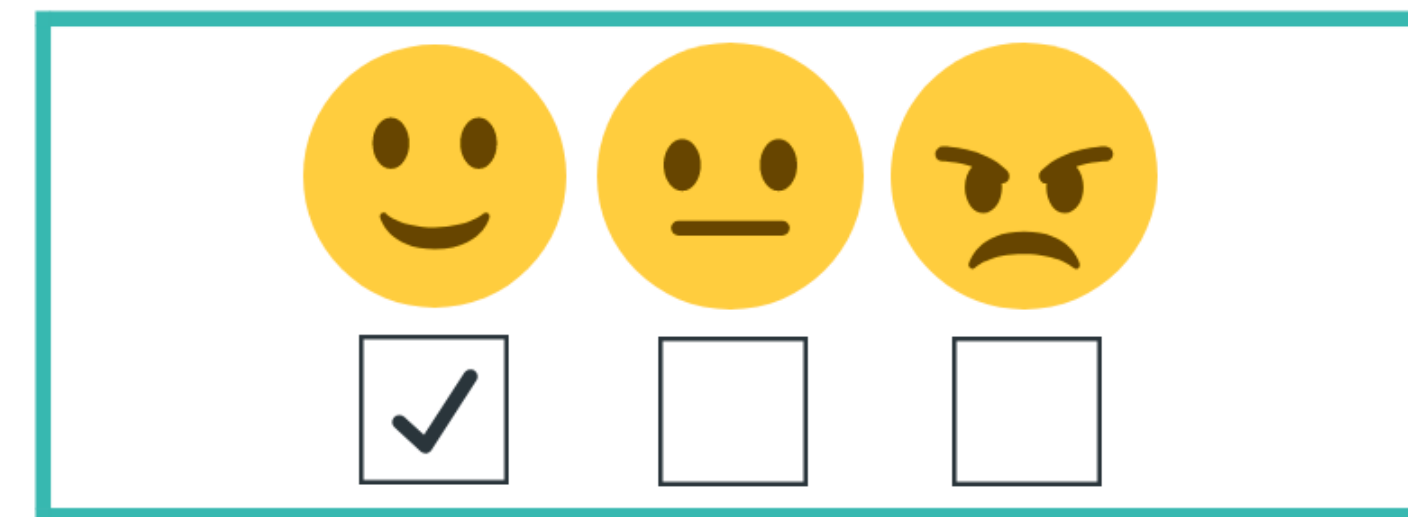


- We will do **Supervised Text Classification**

Why classify?



Spam detection



Sentiment analysis

Movie Reviews

neg: unbelievably disappointing

pos: Full of zany characters and richly applied satire, and some great plot twists

pos: this is the greatest screwball comedy ever filmed

neg: It was pathetic. The worst part about it was the boxing scenes.

- Authorship attribution
- Language detection
- News categorization

Classification as a subtask in NLP

- NLP is all (mostly) about classification
 - Text classification: Spam/Not Spam, Sentiment Analysis
 - **Language modelling / generating sentences:** select word to generate at each step (classification over vocabulary!)
 - Building dialog system (identifying intent)
 - Parsing (identifying word to attach to)

Classification as a subtask in NLP

Intent detection

ADDR_CHANGE: I just moved and want to change my address.

ADDR_CHANGE: Please help me update my address

FILE_CLAIM: I just got into a terrible accident and I want to file a claim

CLOSE_ACCOUNT: I'm moving and I want to disconnect my service

Prepositional phrase attachment

noun attach: *I bought **the shirt** with pockets*

verb attach: *I **bought** the shirt with my credit card*

noun attach: *I washed **the shirt** with mud*

verb attach: *I **washed** the shirt with soap*

Text classification: the task

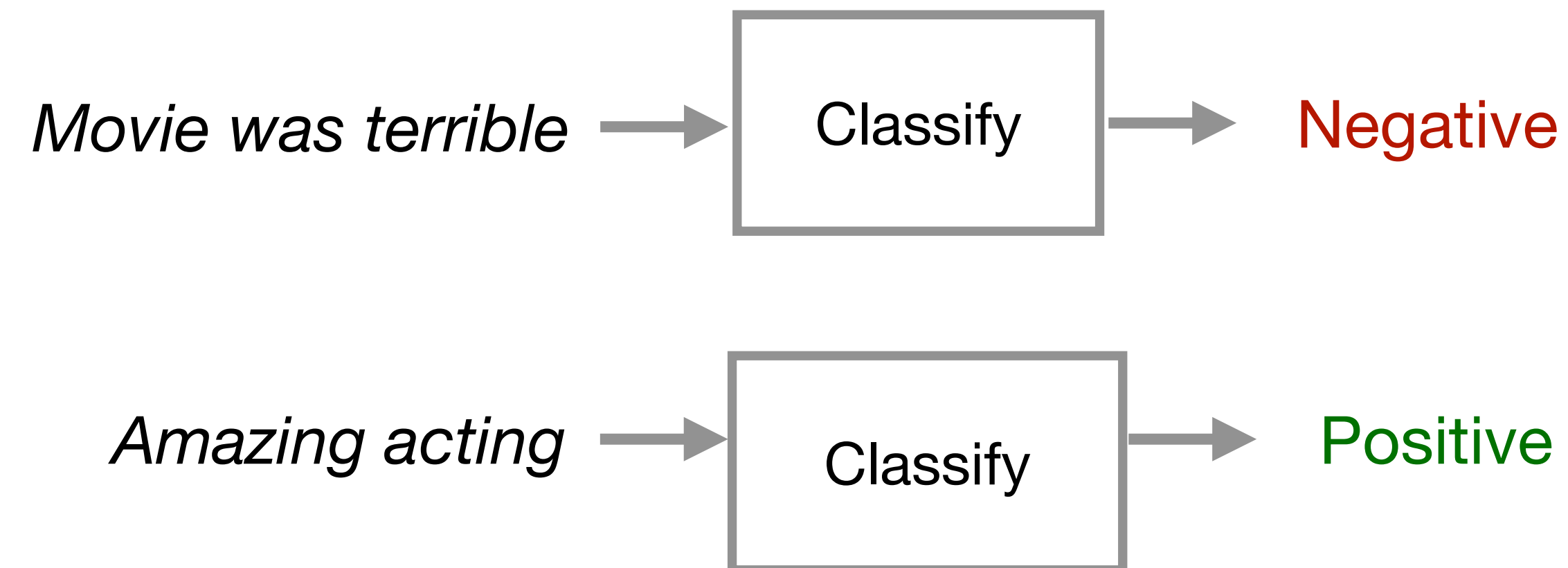
- Inputs:

- A document **d**
- A set of classes **C** = {**c**₁, **c**₂, **c**₃, ..., **c**_m}

Multiple classes: m
Binary: m=2

- Output:

- Predicted class **c** for document **d**



sequence of words
sentence

Rule-based classification

- Look for patterns, and combinations of features on words in document, meta-data

IF there exists word w in document d such that w in [good, great, extra-ordinary, ...],
THEN output **Positive**

IF email address ends in [*ithelpdesk.com*, *makemoney.com*, *spinthewheel.com*, ...]
THEN output **SPAM**

- Simple, can be very accurate
- But: rules may be hard to define (and some even unknown to us!)
 - Expensive
 - Not easily generalizable

Supervised Learning: Let's use statistics!

- Data-driven approach

Let the machine figure out the best patterns to use!

- Inputs:

- Set of m classes $C = \{c_1, c_2, \dots, c_m\}$
- Set of n 'labeled' documents: $\{(d_1, c_1), (d_2, c_2), \dots, (d_n, c_n)\}$

- Output: Trained classifier, $F : d \rightarrow c$

- What form should F take?
- How to learn F ?

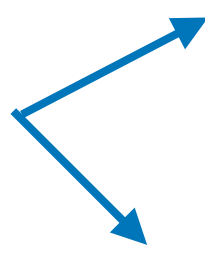


Designing machine learning models

general recipe

- Input **features**: $f(x) \rightarrow [f_1, f_2, \dots, f_m]$
 - Need to determine features
- Output: estimate $P(y | x)$ for each class c
 - Need to model $P(y | x)$ with a **family of functions**
- Train phase: Learn **parameters** of model to minimize loss function
 - Need **training objective** and **optimization** algorithm
- Test phase: Apply parameters to predict class given a new input

Building
the model

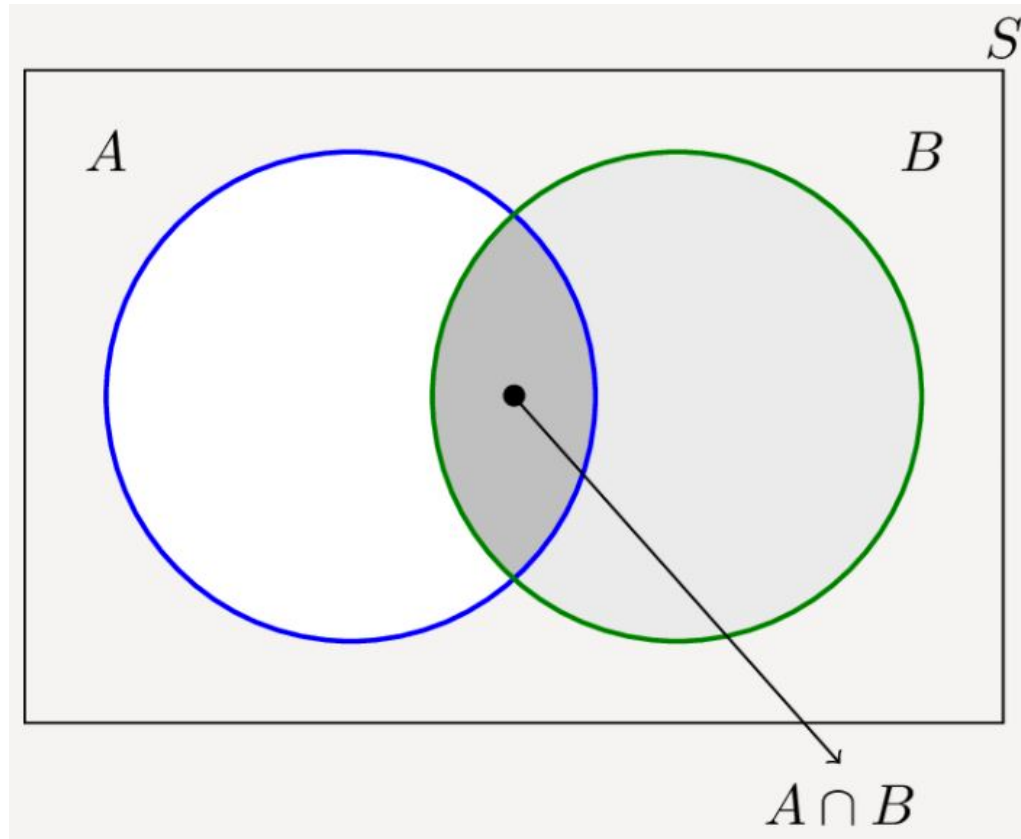


General guidelines for model building

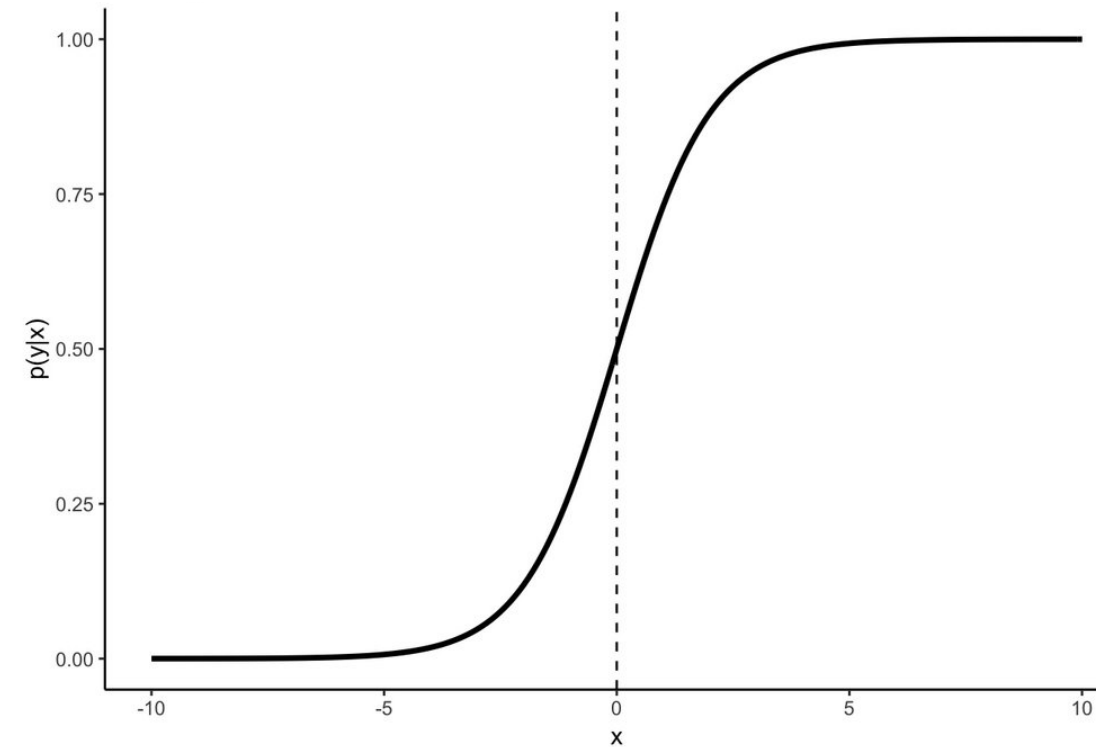
Two steps to building a probability model:

1. Define the model
 - What form should F take?
 - What independence assumptions do we make?
 - What are the model parameters (probability values)?
2. Estimate the model parameters (training/learning)
 - How to learn F ? What to optimize? What is the training objective?

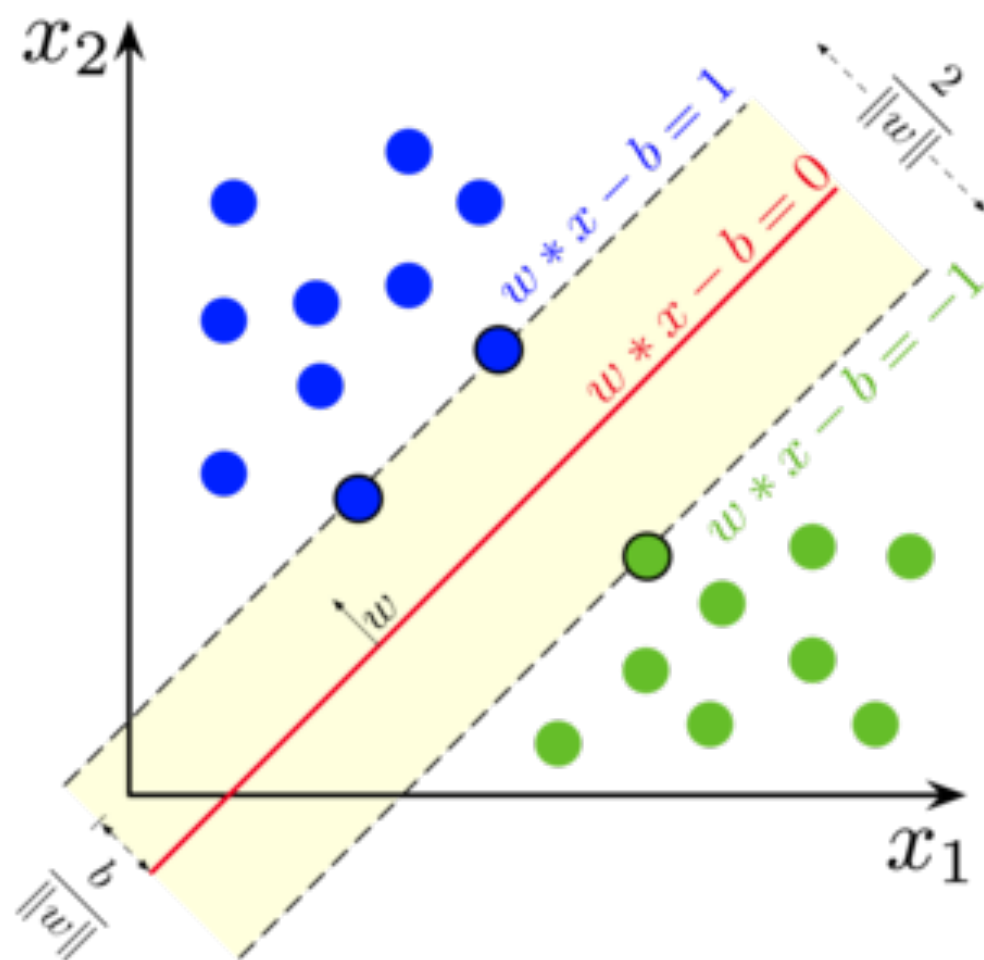
Types of supervised classifiers



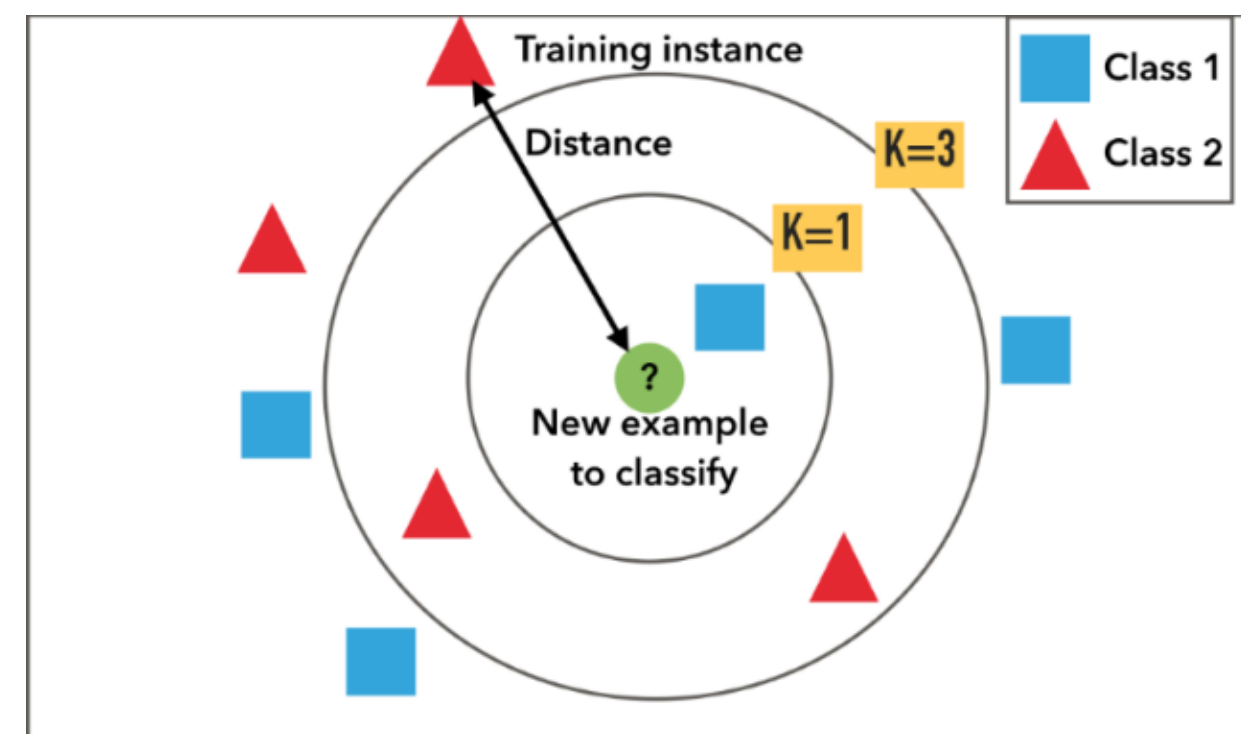
Naive Bayes



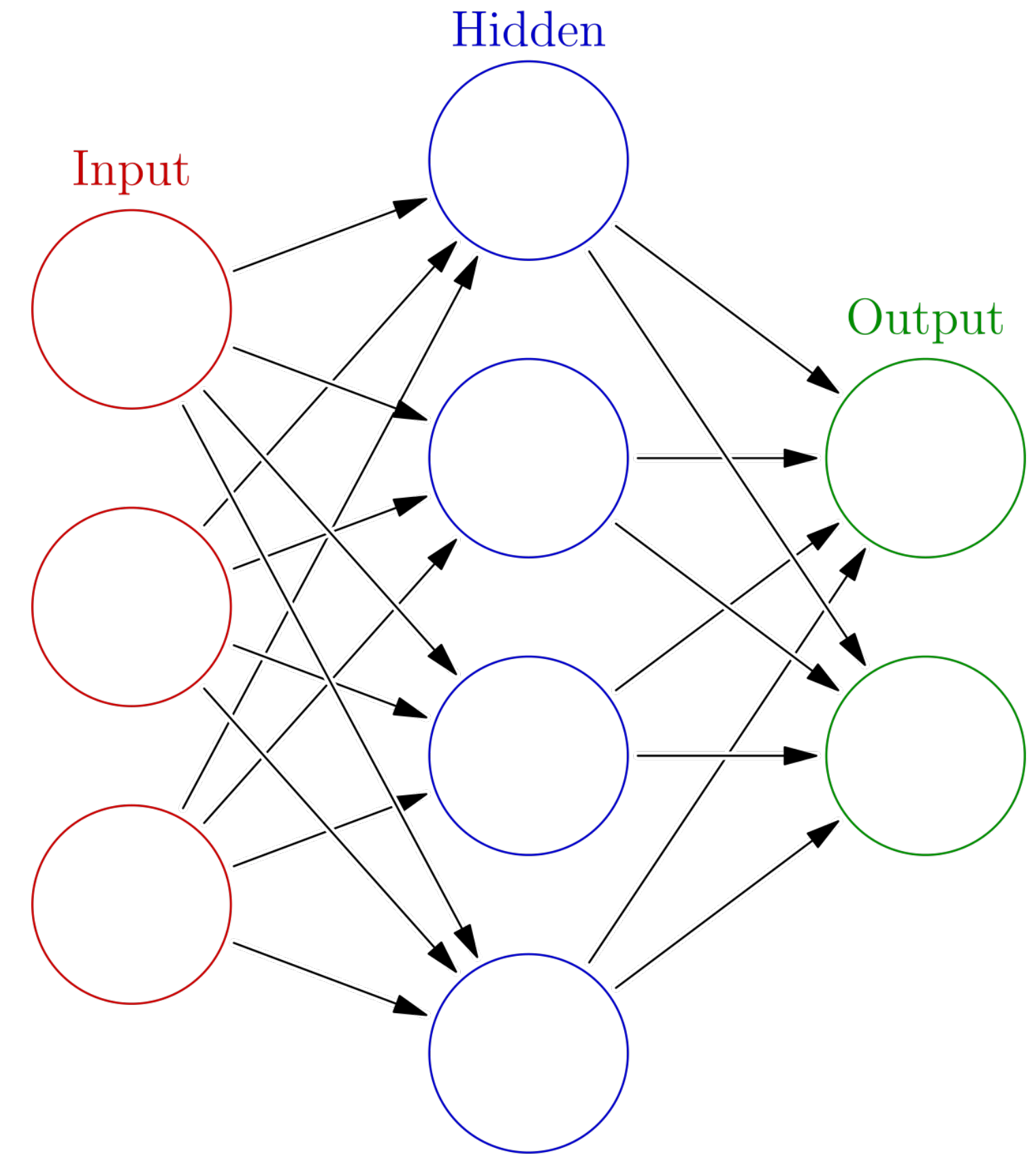
Logistic regression



Support vector machines



k-nearest neighbors



Neural networks

Naive Bayes

Naive Bayes Classifier

General setting

- Let the **input** x be represented as r features: $f_j, 1 \leq j \leq r$
- Let y be the output classification
- We can have a simple classification model using **Bayes rule**

$$\text{Posterior} \quad P(y | x) = \frac{\text{Prior} \quad \text{Likelihood} \quad P(y) \cdot P(x | y)}{P(x) \quad \text{Evidence}}$$

- Make strong (naive) **conditional independence assumptions**

$$P(x | y) = \prod_{j=1}^r P(f_j | y) \xrightarrow{\text{Bayes rule}} P(y | x) \propto P(y) \cdot \prod_{j=1}^r P(f_j | y)$$

Naive Bayes classifier for text classification

- For text classification: input x is document $d = (w_1, \dots, w_k)$
- Use as our features the words w_j , $1 \leq j \leq |V|$ where V is our vocabulary
- c is the output classification
- Predicting the best class:

maximum a posteriori
(MAP) estimate

$C_{\text{MAP}} = \arg \max_{c \in C} P(c | d)$

$$= \arg \max_{c \in C} \frac{P(c)P(d | c)}{P(d)}$$
$$= \arg \max_{c \in C} P(c)P(d | c)$$

$P(d | c) \rightarrow$ Conditional probability of
generating document d from class c

$P(c) \rightarrow$ Prior probability of class c

Represent $P(d | c)$ as Bag of Words model

- Assume position of each word is irrelevant (both absolute and relative) Order doesn't matter
- $P(w_1, w_2, w_3, \dots, w_k | c) = P(w_1 | c)P(w_2 | c) \dots P(w_k | c)$
- Probability of each word is conditionally independent given class c

mat the
sat cat
the



Predicting with Naive Bayes

- Once we assume that the position of each word is irrelevant and that the words are **conditionally independent** given class c , we have:

$$P(d | c) = P(w_1, w_2, w_3, \dots, w_k | c) = P(w_1 | c)P(w_2 | c) \dots P(w_k | c)$$

- The **maximum a posteriori** (MAP) estimate is now:

$\hat{P}$ is used to indicate the estimated probability

$$c_{\text{MAP}} = \arg \max_{c \in C} P(c)P(d | c) = \arg \max_{c \in C} \hat{P}(c) \prod_{i=1}^k \hat{P}(w_i | c)$$

Note that k is the number of tokens (words) in the document.

The index i is the position of the token.

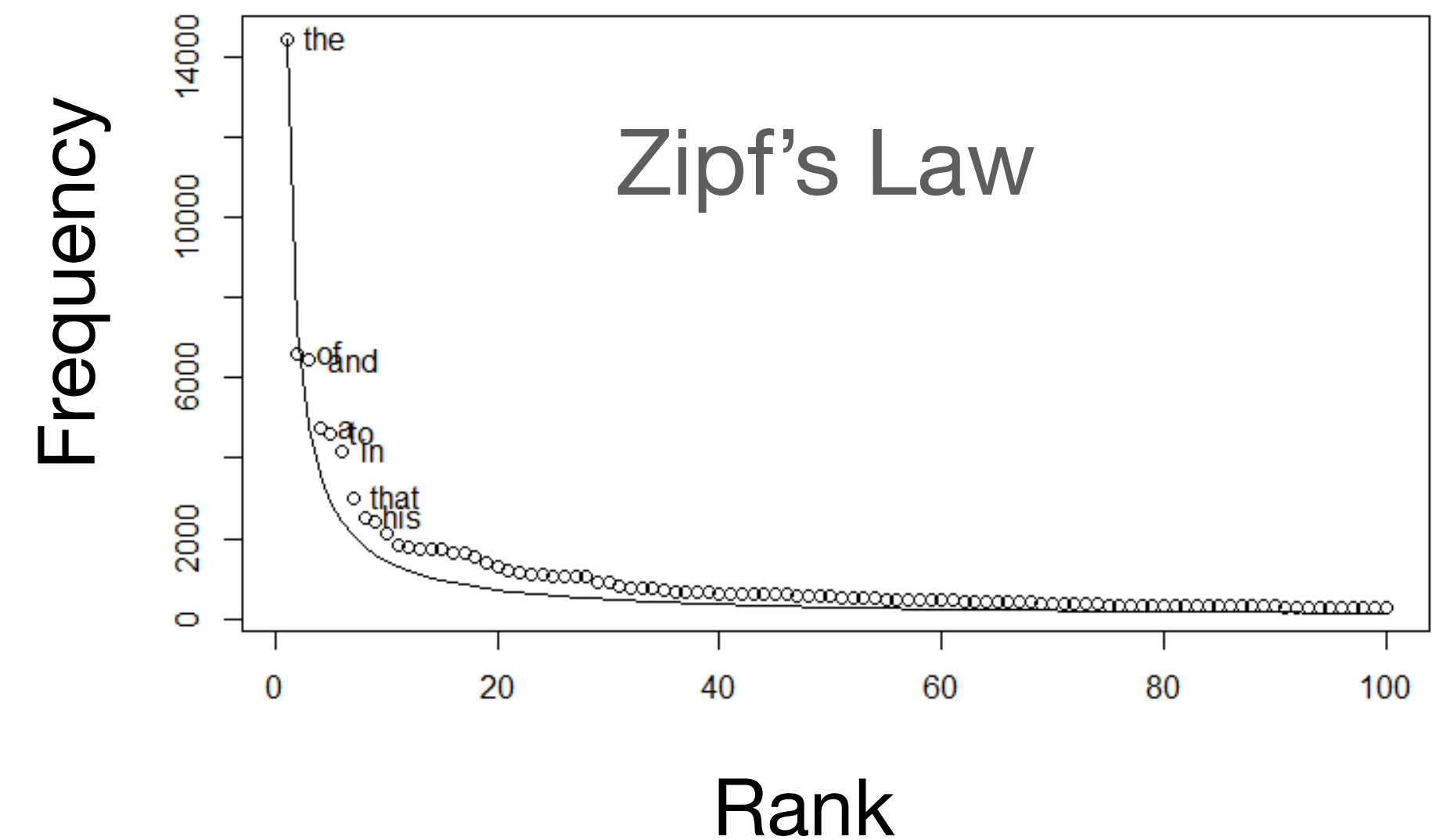
Maximum likelihood estimate

- Count and take average:

$$\hat{P}(c_j) = \frac{\text{Count}(c_j)}{n}$$

$$\hat{P}(w_i|c_j) = \frac{\text{Count}(w_i, c_j)}{\sum_{w \in V} [\text{Count}(w, c_j)]}$$

Can suffer from sparsity issues!



Solution: Smoothing!

- Maximum likelihood estimate

$$\hat{P}(c_j) = \frac{\text{Count}(c_j)}{n}$$

$$\hat{P}(w_i|c_j) = \frac{\text{Count}(w_i, c_j)}{\sum_{w \in V} [\text{Count}(w, c_j)]}$$

- Smoothing

$$\hat{P}(w_i|c_j) = \frac{\text{Count}(w_i, c_j) + \alpha}{\sum_{w \in V} [\text{Count}(w, c_j) + \alpha]}$$

Laplace smoothing

- Simple, easy to use
- Effective in practice

Overall process

- Input: Set of annotated documents $\{(d_i, c_i)\}_{i=1}^n$

A. Compute vocabulary $\mathbf{V}$ of all words

B. Calculate
$$\hat{P}(c_j) = \frac{\text{Count}(c_j)}{n}$$

C. Calculate
$$\hat{P}(w_i|c_j) = \frac{\text{Count}(w_i, c_j) + \alpha}{\sum_{w \in V} [\text{Count}(w, c_j) + \alpha]}$$

D. (Prediction) Given document $d = (w_1, w_2, \dots, w_k)$

$$c_{\text{MAP}} = \arg \max_c \hat{P}(c) \prod_{i=1}^k \hat{P}(w_i|c)$$

Variants

Name based on the distribution of the features

$$P(f_i|y) \rightarrow P(w_i|c)$$

Multinomial Naive Bayes

Normal counts (0,1,2,...) for each document

$$\hat{P}(c_j) = \frac{\text{Count}(c_j)}{n}$$

Binary Multinomial NB

Binarized counts (0/1) for each document

Some work show this works better than full counts or the Multivariate Bernoulli NB

Multivariate Bernoulli NB

Estimate $P(w|c)$ as fraction of documents of class c with word w

- Explicitly model $P(!w|c) = 1 - P(w|c)$

Variants

Name based on the distribution of the features $P(f_i|y) \rightarrow P(w_i|c)$

Multinomial Naive Bayes

Normal counts (0,1,2,...) for each document $\hat{P}(c_j) = \frac{\text{Count}(c_j)}{n}$

Binary Multinomial NB

Binarized counts (0/1) for each document

Multivariate Bernoulli NB

Estimate $P(w|c)$ as fraction of documents of class c with word w

- Explicitly model $P(!w|c) = 1 - P(w|c)$

Naive Bayes Example

$$\hat{P}(c) = \frac{N_c}{N}$$

Smoothing with $\alpha = 1$

$$\hat{P}(w | c) = \frac{\text{count}(w, c) + 1}{\text{count}(c) + |V|}$$

	Doc	Words	Class
Training	1	Chinese Beijing Chinese	c
	2	Chinese Chinese Shanghai	c
	3	Chinese Macao	c
	4	Tokyo Japan Chinese	j
Test	5	Chinese Chinese Chinese Tokyo Japan	?

Priors:

$$P(c) =$$

$$P(j) =$$

Choosing a class:

$$P(c | d5) \propto$$

Conditional Probabilities:

$$P(\text{Chinese} | c) =$$

$$P(\text{Tokyo} | c) =$$

$$P(\text{Japan} | c) =$$

$$P(\text{Chinese} | j) =$$

$$P(\text{Tokyo} | j) =$$

$$P(\text{Japan} | j) =$$

$$P(j | d5) \propto$$

(Credits: Dan Jurafsky)

Naive Bayes Example

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- Let's compute the priors: what is $\hat{P}(c)$ and $\hat{P}(j)$? $\hat{P}(c) = \frac{3}{4}, \hat{P}(j) = \frac{1}{4}$

- Let's compute $\hat{P}(\text{Japan} | c)$:

$$\text{count}(\text{Japan}, c) = 0 \quad \text{count}(c) = \sum_{w \in V} \text{count}(w, c) = 8 \quad |V| = 6$$

$$\hat{P}(\text{Japan} | c) = \frac{\text{count}(\text{Japan}, c) + 1}{\text{count}(c) + |V|}$$

(Credits: Dan Jurafsky)

Naive Bayes Example

$$\hat{P}(c) = \frac{N_c}{N}$$

Smoothing with $\alpha = 1$

$$\hat{P}(w | c) = \frac{\text{count}(w, c) + 1}{\text{count}(c) + |V|}$$

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$$P(\text{Tokyo} | j) =$$

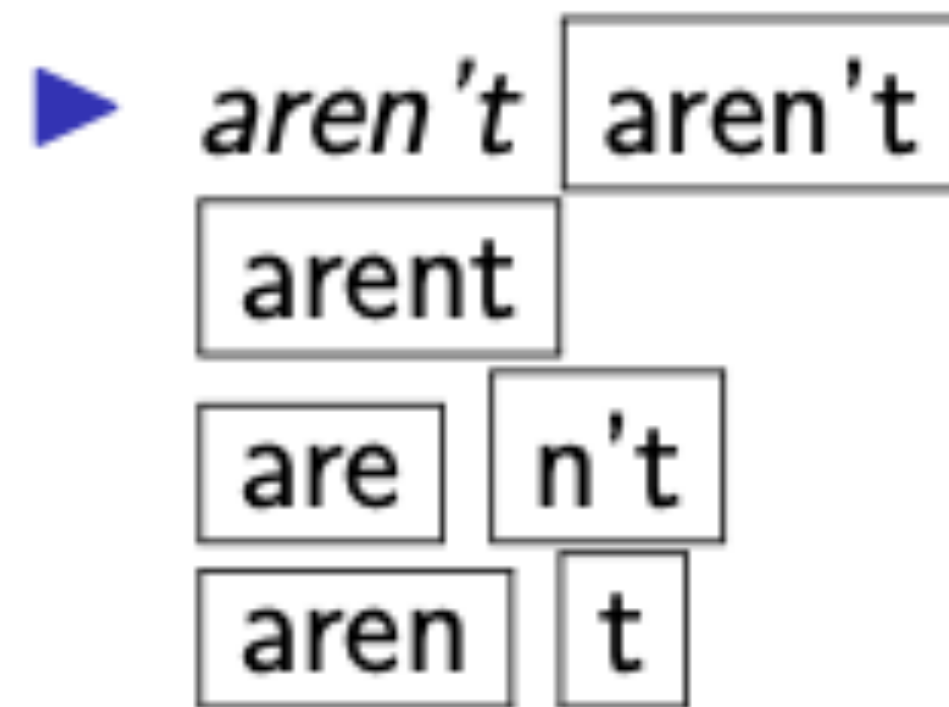
$$P(\text{Japan} | j) =$$

$$P(j | d5) \propto$$

(Credits: Dan Jurafsky)

Some details

- **Vocabulary** is important
- **Tokenization** matters: it can affect your **vocabulary**
 - Tokenization = how you break your sentence up into tokens / words
 - Make sure you are consistent with your tokenization!



► Emails, URLs, phone numbers, dates, emoticons

- Special multi-word tokens: NOT_happy
- Modern NLP system use **subword tokens** (e.g. byte pair encoding)

Some details

- **Vocabulary** is important
 - **Tokenization** matters: it can affect your **vocabulary**
 - Tokenization = how you break your sentence up into tokens / words
 - Make sure you are consistent with your tokenization!
 - Handling **unknown** words in test not in your training vocabulary?
 - Remove them from your test document! Just ignore them.
 - Handling **stop** words (common words like *a*, *the* that may not be useful)
 - Remove them from the training data!
 - In practice not that helpful, so use all words!
- Better to use
- Modified counts (tf-idf) that down weighs frequent, unimportant words
 - **Better models!**

Features

- In general, Naive Bayes can use **any set of features**, not just words
- URLs, email addresses, Capitalization, ...
- Domain knowledge can be crucial to performance

*Top features
for
Spam detection*

Rank	Category	Feature	Rank	Category	Feature
1	Subject	Number of capitalized words	1	Subject	Min of the compression ratio for the bz2 compressor
2	Subject	Sum of all the character lengths of words	2	Subject	Min of the compression ratio for the zlib compressor
3	Subject	Number of words containing letters and numbers	3	Subject	Min of character diversity of each word
4	Subject	Max of ratio of digit characters to all characters of each word	4	Subject	Min of the compression ratio for the lzw compressor
5	Header	Hour of day when email was sent	5	Subject	Max of the character lengths of words
(a)			(b)		
Spam URLs Features					
1	URL	The number of all URLs in an email	1	Header	Day of week when email was sent
2	URL	The number of unique URLs in an email	2	Payload	Number of characters
3	Payload	Number of words containing letters and numbers	3	Payload	Sum of all the character lengths of words
4	Payload	Min of the compression ratio for the bz2 compressor	4	Header	Minute of hour when email was sent
5	Payload	Number of words containing only letters	5	Header	Hour of day when email was sent

Properties of Naive Bayes

- + Simple baseline method
- + Works well for small data sizes
- + Optimal if the independence assumptions hold: if the assumed independence is correct, then it is the Bayes Optimal Classifier for the problem
 - But not if the independence assumption is broken
 - Does not handle rare classes well - will favour more common class
 - Also need to design features
- **Modern NLP: use large neural language models with learned representations**

Generative vs Discriminative Models

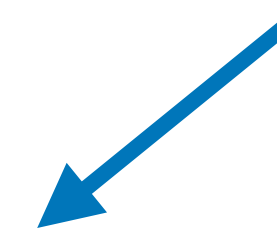
- Naive Bayes is a Generative Model: It models $p(y | x) \propto p(y)p(x | y)$
- It models how the document is generated from words
- You can use this model to sample documents
- Next: Logistic Regression, a Discriminative model that models $p(y | x)$ directly.

Evaluation

Evaluation

- Consider binary classification
- Table of predictions

Confusion matrix



		<i>Truth</i>	
		Positive	Negative
<i>Predicted</i>	Positive	100	5
	Negative	45	100

- Ideally, we want:

		<i>Truth</i>	
		Positive	Negative
<i>Predicted</i>	Positive	145	0
	Negative	0	105

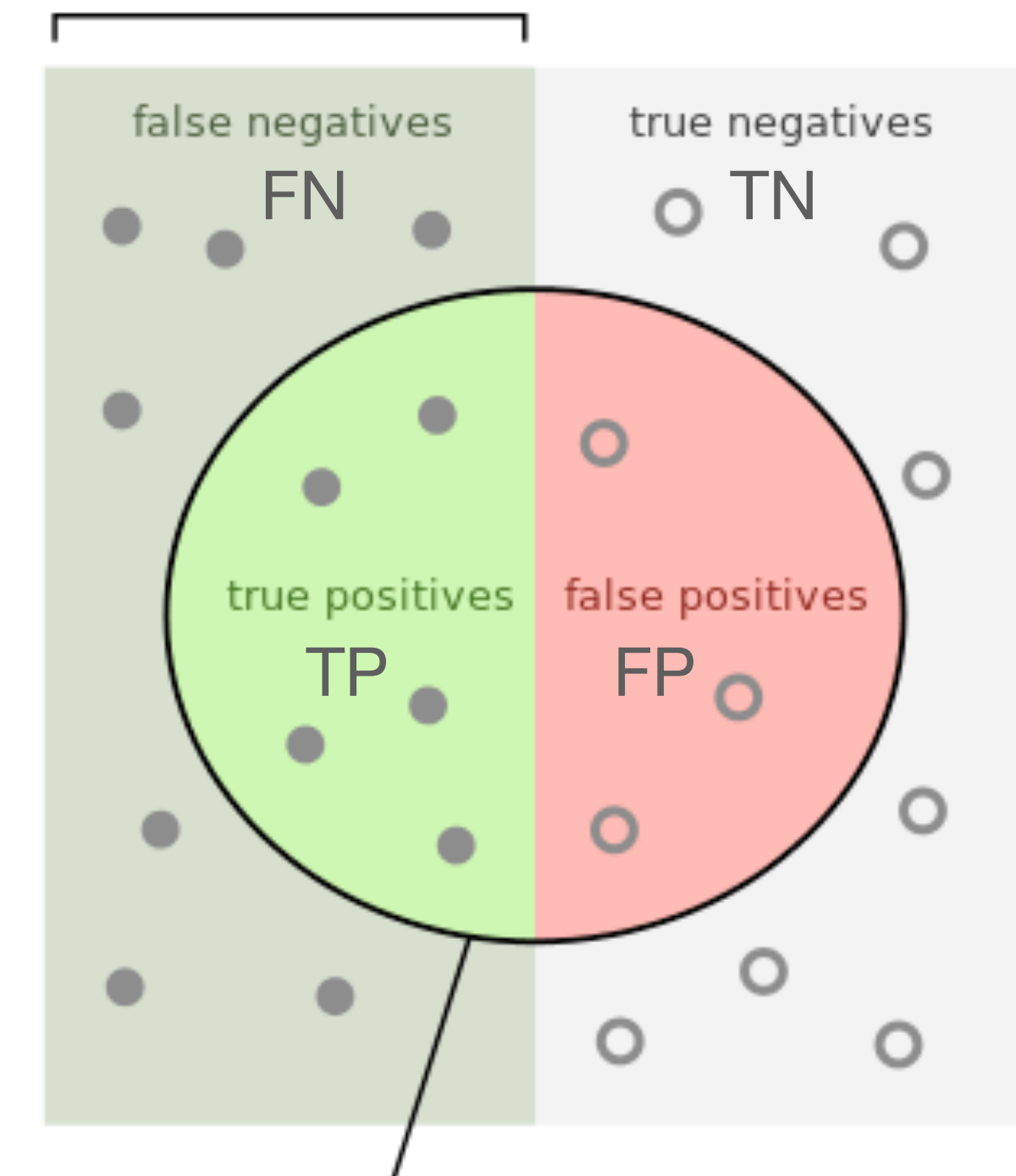
Evaluation Metrics

Confusion matrix

		Truth	
		Positive	Negative
Predicted	Positive	100 TP	5 FP
	Negative	45 FN	100 TN

- True positive (TP): Predicted + and actual +
- True negative (TN): Predicted - and actual -
- False positive (FP): Predicted + and actual -
- False negative (FN): Predicted - and actual +

Actual positives



Predicted positives

(image credit: wikipedia)

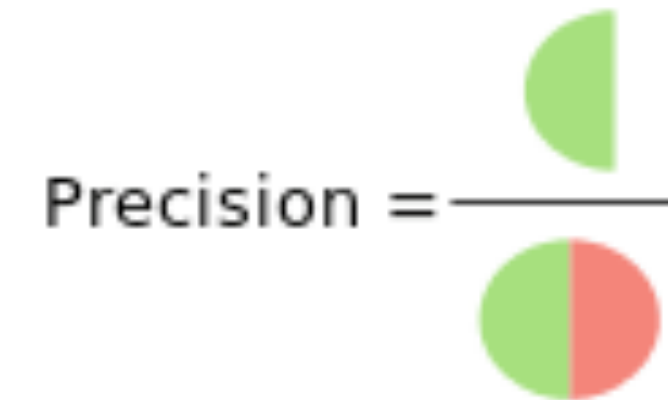
$$\text{Accuracy} = \frac{TP + TN}{\text{Total}} = \frac{200}{250} = 80 \%$$

Coarse metric

Precision and Recall

- Precision: % of selected classes that are correct

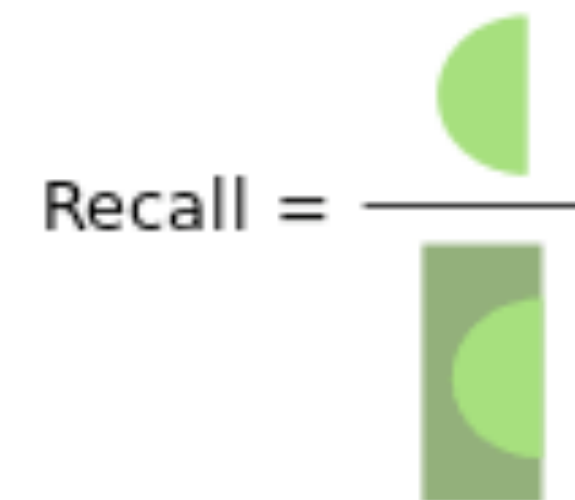
$$\text{Precision}(+) = \frac{TP}{TP + FP}$$



$$\text{Precision} = \frac{\text{Intersection}}{\text{TP} + \text{FP}}$$

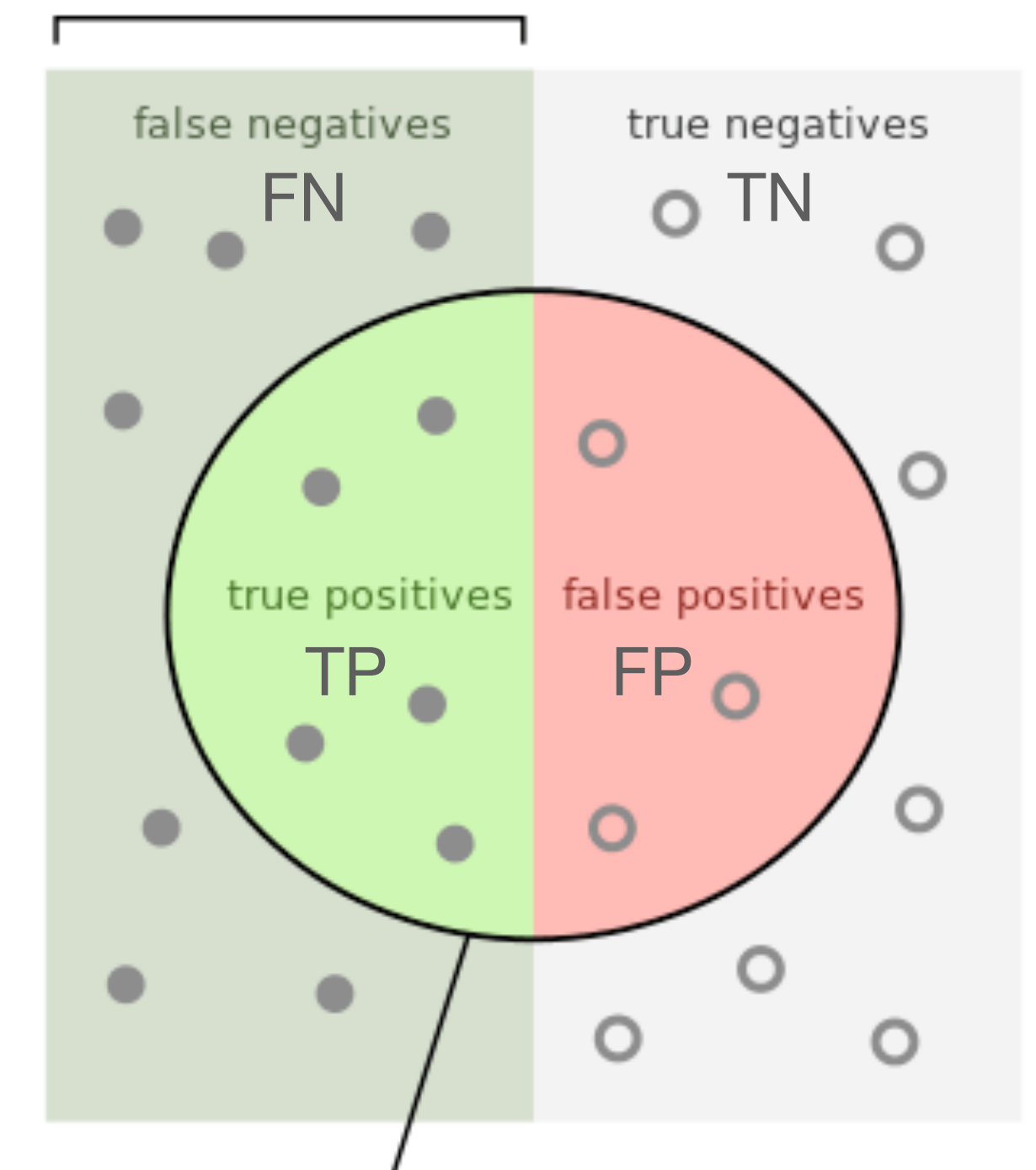
- Recall: % of correct items selected

$$\text{Recall}(+) = \frac{TP}{TP + FN}$$



$$\text{Recall} = \frac{\text{Intersection}}{\text{TP} + \text{FN}}$$

Actual positives (relevant)



Predicted positives
(selected/retrieved)

(image credit: wikipedia)

Evaluation Metrics

		<i>Truth</i>	
		Positive	Negative
<i>Predicted</i>	Positive	100	5
	Negative	45	100

		Positive	Negative
	Positive	50	25
	Negative	25	150

$$\text{Precision}(+) = \frac{TP}{TP + FP}$$

$$\frac{100}{100 + 5} = 0.95$$

$$\frac{50}{50 + 25} = 0.75$$

$$\text{Recall}(+) = \frac{TP}{TP + FN}$$

$$\frac{100}{100 + 45} = 0.69$$

$$\frac{50}{50 + 25} = 0.75$$

Two metrics - which one to use?

F-Score

- Combined measure
- Harmonic mean of Precision and Recall

$$F_1 = \frac{2 \cdot \text{Precision} \cdot \text{Recall}}{\text{Precision} + \text{Recall}}$$

- Or more generally,



Use β to control importance of Precision vs Recall

$$F_\beta = \frac{(1 + \beta^2) \cdot \text{Precision} \cdot \text{Recall}}{\beta^2 \cdot \text{Precision} + \text{Recall}}$$

Evaluation Metrics

		Truth	
		Positive	Negative
Predicted	Positive	100	5
	Negative	45	100

		Truth	
		Positive	Negative
Predicted	Positive	50	25
	Negative	25	150

$$\text{Precision}(+) = \frac{TP}{TP + FP}$$

$$\frac{100}{100 + 5} = 0.95$$

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$$\text{Recall}(+) = \frac{TP}{TP + FN}$$

$$\frac{100}{100 + 45} = 0.69$$

$$\frac{50}{50 + 25} = 0.75$$

$$F_1(+) = \frac{2 \cdot P(+)R(+)}{P(+) + R(+)}$$

$$0.8$$

$$0.75$$

Aggregating scores

- How to handle more than 2 classes?
- We have Precision, Recall, F1 for each class

		<i>gold labels</i>			
		urgent	normal	spam	
<i>system output</i>	urgent	8	10	1	$\text{precision}_u = \frac{8}{8+10+1}$
	normal	5	60	50	$\text{precision}_n = \frac{60}{5+60+50}$
	spam	3	30	200	$\text{precision}_s = \frac{200}{3+30+200}$
		$\text{recall}_u = \frac{8}{8+5+3}$	$\text{recall}_n = \frac{60}{10+60+30}$	$\text{recall}_s = \frac{200}{1+50+200}$	

(Credits: Dan Jurafsky)

Aggregating scores

- How to handle more than 2 classes?
- We have Precision, Recall, F1 for each class
- How to combine them for an overall score?
- **Macro-average**: Compute for each class, then average
- **Micro-average**: Collect predictions for all classes and jointly evaluate

Macro vs Micro average

- Micro-averaged score is dominated by score on **common** classes

Class 1: Urgent

	true urgent	true not
system urgent	8	11
system not	8	340

$$\text{precision} = \frac{8}{8+11} = .42$$

Class 2: Normal

	true normal	true not
system normal	60	55
system not	40	212

$$\text{precision} = \frac{60}{60+55} = .52$$

Class 3: Spam

	true spam	true not
system spam	200	33
system not	51	83

$$\text{precision} = \frac{200}{200+33} = .86$$

$$\text{macroaverage precision} = \frac{.42+.52+.86}{3} = .60$$

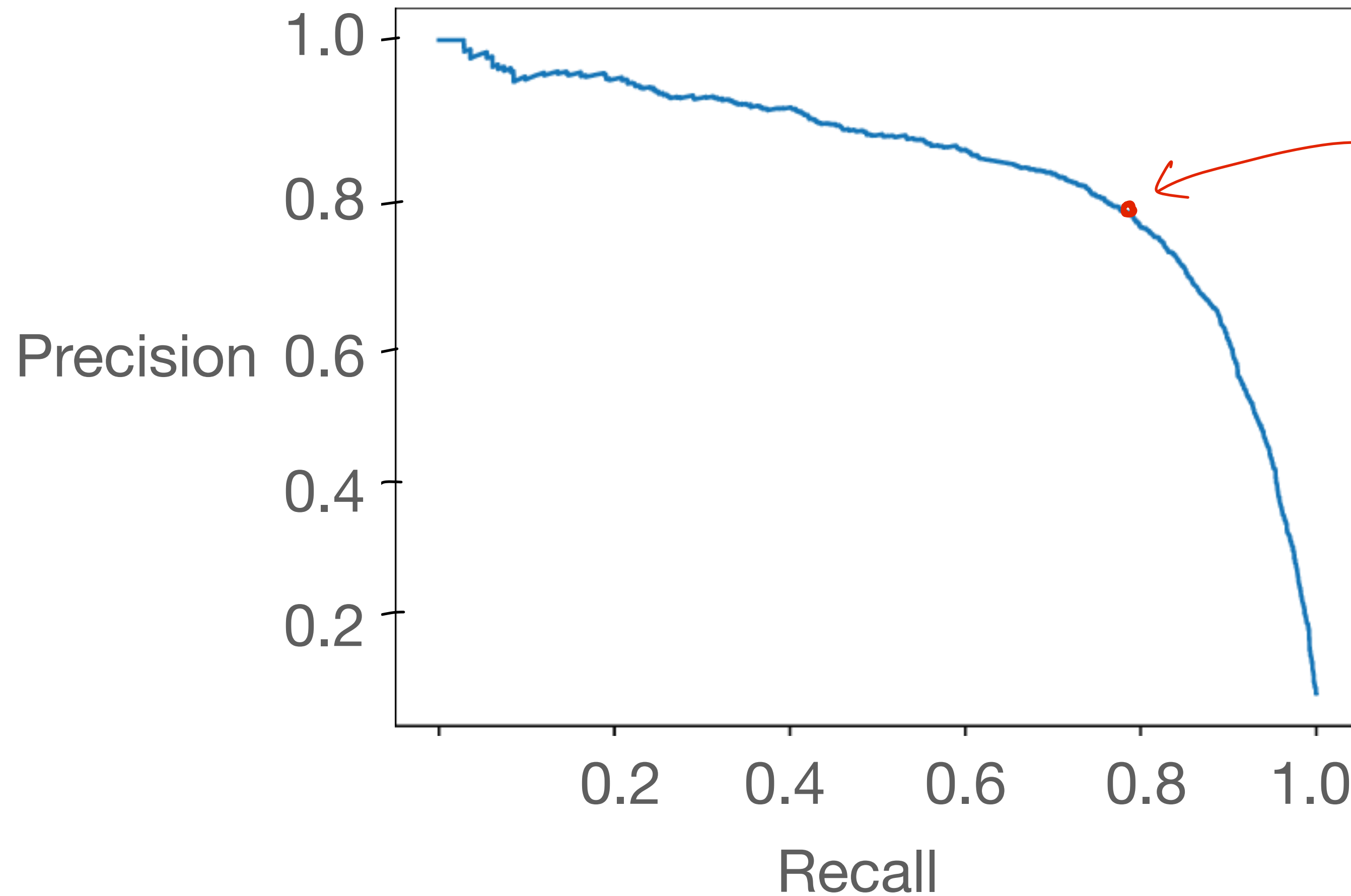
Pooled

	true yes	true no
system yes	268	99
system no	99	635

$$\text{microaverage precision} = \frac{268}{268+99} = .73$$

(Credits: Dan Jurafsky)

Precision Recall tradeoff



Maximum F1

Vary hyperparameters

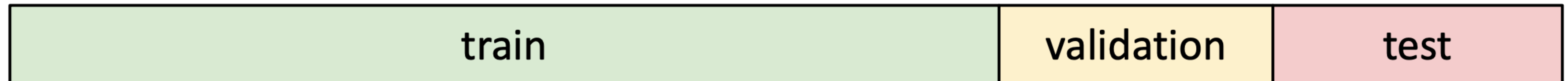
- Smoothing α
- Threshold T

$$\frac{P(+ | d)}{P(- | d)} > T$$

Tune on validation set

Train, val, test split

- Train model on **training** set
- Tune hyperparameters on **validation** set
- Evaluate performance on unseen **test** set



Why do we do this?

Summary

- Evaluation Metrics
 - **Accuracy** - coarse metric
 - **Precision**, **Recall**, **F1** for each class
- Aggregated scores
 - **Macro-average**: Compute for each class, then average
 - **Micro-average**: Collect predictions for all classes and jointly evaluate (dominated by common classes)
- Precision-Recall curve: pick threshold for maximum F1
 - Use **validation** set to tune hyperparameters, **test** set should remain “unseen”